## CANDIDATE NAME

CENTRE
CANDIDATE NUMBER
 NUMBER

## MATHEMATICS (SYLLABUS D)

4024/11
Paper 1
May/June 2010
2 hours
Candidates answer on the Question Paper.
Additional Materials: Geometrical instruments

## READ THESE INSTRUCTIONS FIRST

Write your Centre number, candidate number and name on all the work you hand in.
Write in dark blue or black pen.
You may use a pencil for any diagrams or graphs.
Do not use staples, paper clips, highlighters, glue or correction fluid.
DO NOT WRITE IN ANY BARCODES.
Answer all questions.
If working is needed for any question it must be shown in the space below that question.
Omission of essential working will result in loss of marks.

## NEITHER ELECTRONIC CALCULATORS NOR MATHEMATICAL TABLES MAY BE USED IN THIS PAPER.

The number of marks is given in brackets [ ] at the end of each question or part question.
The total of the marks for this paper is 80 .


This document consists of $\mathbf{2 0}$ printed pages.

International Examinations

## NEITHER ELECTRONIC CALCULATORS NOR MATHEMATICAL TABLES MAY BE USED IN THIS PAPER.

1 Evaluate
(a) $\frac{1}{2}+\frac{2}{9}$,

Answer (a)
(b) $\frac{2}{3} \div \frac{9}{11}$.

2 (a) Evaluate $10-8 \div 2+3$.

Answer (a)
(b) Find $20 \%$ of 60 cm .

3 Sara carries out a survey of the colours of cars in a car park. She draws a pie chart to represent her results.
(a) There are 7 red cars.

The angle representing the red cars is $40^{\circ}$.
Calculate the total number of cars in the car park.

Answer (a)
(b) Sara's pie chart is a circle with circumference 28 cm .

Find, in terms of $\pi$, the diameter of the circle.

Answer (b)
cm [1]

4 Ed goes on a car journey.
The first 60 km of the journey takes 45 minutes.
The remaining 20 km of the journey takes 30 minutes.
Calculate his average speed, in kilometres per hour, for the whole journey.


The bearing of a lighthouse from a ship, S , is $220^{\circ}$.
The position of $S$ is marked on the diagram.
(a) Which of the four points $\mathrm{A}, \mathrm{B}, \mathrm{C}$ or D is a possible position of the lighthouse?
Answer
(a)
(b) Write down the bearing of S from the lighthouse.

6 (a) Solve $6 x-5<9+2 x$.

Answer (a)
(b) Write down the largest integer which satisfies the inequality

$$
6 x-5<9+2 x .
$$

7 Given that $n$ is an integer and $\boldsymbol{n}>\mathbf{1}$, decide whether each statement in the table is true or false.
For each statement write true or false in the table. If you write false, give an example to justify your decision.

| Statement | True or False | Example (if false) |
| :---: | :--- | :--- |
| $n^{3}>1$ |  |  |
| $\frac{1}{n}>\frac{1}{n^{2}}$ |  |  |
| $(n-1)(n+3)$ <br> is always odd |  |  |

8 (a) The ratio of Sayed's age to his mother's age is 2:7.
Sayed is 14 years old.
How old is his mother?

Answer (a) .years [1]
(b) The ratio of Fatima's age to her father's age is $3: 8$.

The total of their ages is 66 years.
How old is Fatima?

Answer (b)
.years [1]


Pencils are packed in a box.
Each pencil has a diameter of 7 mm , correct to the nearest millimetre.
(a) Write down the lower bound of the diameter of a pencil.

Answer (a) $\qquad$ .mm [1]
(b) Find the smallest width of a box that can always hold 8 pencils side by side.

Give your answer in centimetres.

10 Evaluate
(a) $0.2 \times 0.06$,
(b) $3 \div 0.01$,

Answer (b)
(c) $27^{\frac{1}{3}}$.

Answer (c)

11


The diagram shows two circles, both with centre $O$.
$C D$ is a diameter of the small circle and $A B$ is a diameter of the large circle.

Using congruent triangles, show that $B D=A C$.
State your reasons clearly.
In triangles
and
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$

12


In the diagram, the region, $\mathbf{R}$, is bounded by the lines $A B, B C, C D$ and $D A$.
(a) Write down the coordinates of the midpoint of $A B$.

Answer (a) (.........., ...........) [1]
(b) Region $\mathbf{R}$ is defined by four inequalities.

One of these is $y \leqslant x+5$.
Write down the other three inequalities.

Answer (b) $\qquad$
$\qquad$
$\qquad$

13 Two families ordered three basic food items from their local shop.
The Jones family ordered 1 bag of sugar, 4 cartons of milk and 3 loaves of bread.
The Singh family ordered no sugar, 3 cartons of milk and 5 loaves of bread.
Their orders can be represented by the matrix $\mathbf{A}$ where

$$
\mathbf{A}=\left(\begin{array}{ll}
1 & 0 \\
4 & 3 \\
3 & 5
\end{array}\right)
$$

The cost of a bag of sugar is 80 cents, the cost of a carton of milk is 50 cents and the cost of a loaf of bread is 40 cents.
This information can be represented by the matrix $\mathbf{B}$ where

$$
\mathbf{B}=\left(\begin{array}{lll}
80 & 50 & 40
\end{array}\right) .
$$

(a) Work out BA.

Answer (a)
[2]
(b) What does the matrix BA represent?

Answer (b) $\qquad$
$\qquad$
$\qquad$
$\qquad$

14 Ida keeps a record of time spent on the internet each day.
Her results are summarised in the table.

| Time $(t$ minutes $)$ | Frequency |
| :---: | :---: |
| $0 \leqslant t<10$ | 4 |
| $10 \leqslant t<30$ | 20 |
| $30 \leqslant t<60$ | 39 |
| $60 \leqslant t<100$ | 32 |
| $100 \leqslant t<120$ | 6 |

On the axes below, draw a histogram to show these results.


15 Ahmed goes shopping.
(a) In one shop he buys shorts for $\$ 26.84$ and a shirt for $\$ 13.97$.

How much does Ahmed spend altogether?

Answer (a) \$ .
[1]
(b) In another shop he buys 15 postcards for 46 cents each.
(i) Calculate the total cost, in dollars, of the postcards.

Answer (b)(i) \$.
(ii) The rate of exchange between pounds $(£)$ and dollars $(\$)$ was $£ 1=\$ 2.50$.

Calculate the total cost of the postcards in pounds.

Answer (b)(ii) £

16 Dai played three games of cricket.
His mean score was 9 runs.
His median score was 8 runs.
His highest score was 7 runs more than his lowest score.
(a) Find the number of runs he scored in each of the three games.

Answer (a)
(b) Dai batted in a fourth game

The mean of his four scores was 11 runs.
Find the number of runs that Dai scored in the fourth game.

Answer (b)
$17 y$ is inversely proportional to $x^{2}$.
Some values of $y$ and $x$ are given in the table below.

| $x$ | 3 | 2 | $q$ |
| :--- | :--- | :--- | :--- |
| $y$ | 4 | $p$ | 1 |

Find
(a) the formula for $y$ in terms of $x$,

Answer (a) $y=$
For Examiner's

Find
[2]
(b) the value of $p$,

Answer (b) $p=$
(c) the two values of $q$.

Answer (c) $q=$.


In the diagram, $A B$ is parallel to $E C$.
$D$ is the point on $E C$ such that $E D=E A$.
$A \hat{B} C=135^{\circ}$ and $A \hat{D} E=65^{\circ}$.
Find
(a) $A \hat{E} D$,

Answer (a) A $\hat{E} D=$
(b) $D \hat{A B}$,

Answer (b) $D \hat{A} B=$
(c) $B \hat{C} D$,

Answer (c) $B \hat{C} D=$
(d) reflex $A \hat{B} C$.

Answer (d) reflex $A \hat{B} C=$

19 Some data about two planets, Earth and Mars, is shown in the table.

| Planet | Average <br> temperature $\left({ }^{\circ} \mathrm{C}\right)$ | Mass <br> (tonnes) | Volume <br> $\left(\mathrm{km}^{3}\right)$ |
| :---: | :---: | :---: | :---: |
| Earth | 15 | $5.98 \times 10^{21}$ | $1.08 \times 10^{12}$ |
| Mars | -63 | $6.58 \times 10^{20}$ | 162000 million |

(a) How much greater is the average temperature on Earth than that on Mars?

Answer (a) $\qquad$ ${ }^{\circ} \mathrm{C}$ [1]
(b) Write down the volume of Mars in standard form.

Answer (b) $\mathrm{km}^{3}$ [1]
(c) Calculate the difference in mass between Earth and Mars. Give your answer in standard form.

Answer (c)
.tonnes [2]


In the diagram, $A C$ and $B D$ intersect at $X$.
Triangle $A B X$ is similar to triangle $C D X$.
$A B=3 \mathrm{~cm}, A X=2 \mathrm{~cm}$ and $X C=5 \mathrm{~cm}$.
(a) Find the ratio of the area of triangle $A B X$ to the area of triangle $C D X$.
$\qquad$ :
(b) Find the ratio of the area of triangle $A B X$ to the area of triangle $B C X$.

Answer (b) $\qquad$ :
(c) Calculate $C D$.

21 (a) Write down, in terms of $n$, an expression for the $n$th term of the sequence

$$
\begin{array}{lllll}
19 & 16 & 13 & 10 & \ldots . . . . . . . . . . ~
\end{array}
$$

Answer (a)
(b) Factorise completely
(i) $4 x^{2}-25 y^{2}$,
(ii) $5 a x-5 a^{2}-2 x+2 a$.

22 A walker leaves his house at 1000 and walks towards a shopping centre at a constant speed of $5 \mathrm{~km} / \mathrm{h}$.
A cyclist leaves the same house 10 minutes later.
He travels along the same road at a constant speed of $20 \mathrm{~km} / \mathrm{h}$ until he reaches the shopping centre which is 6 km from the house.
The cyclist stops at the shopping centre for 14 minutes.
He then returns to the house along the same road at a constant speed of $20 \mathrm{~km} / \mathrm{h}$.
(a) The distance-time graph for the walker is drawn below.

On the same axes, draw the distance-time graph for the cyclist.

(b) Using the graphs, find
(i) the time when the cyclist, on his return journey, meets the walker,

$$
\text { Answer } \quad(b)(\mathrm{i})
$$

(ii) the distance from the house when this meeting takes place.

Answer (b)(ii) $\qquad$ km

23 A stone is thrown vertically upwards from the ground so that its height above the ground after $t$ seconds is $\left(20 t-5 t^{2}\right)$ metres.
(a) (i) Show that the values of $t$ when the stone is 15 metres above the ground satisfy the equation

$$
t^{2}-4 t+3=0
$$

(ii) Find the values of $t$ when the stone is 15 metres above the ground.

Answer (a)(ii) $t=$ $\qquad$ and
(b) Find the value of $t$ when the stone hits the ground.

Answer (b) $t=$

## 24 (a) Solve

(i) $5-2(3 x-1)=2 x+1$,

Answer (a)(i) $x=$ $\qquad$
(ii) $\frac{2}{5 t}=\frac{3}{4}$.

Answer (a)(ii) $t=$
(b) Solve the simultaneous equations

$$
\begin{aligned}
& 5 x-2 y=16 \\
& 2 x-3 y=13
\end{aligned}
$$

$$
\text { Answer (b) } x=
$$

$\qquad$

$$
\begin{equation*}
y= \tag{3}
\end{equation*}
$$

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